

EECS 361  
Test 2 Topics

- 1) Find the Fourier Transform of aperiodic signals
- 2) Find the Fourier Transform of periodic signals
- 3) Find the Fourier Series of a periodic signal using the relationship between Fourier Transform and Fourier Series

$$x_p(t) = \sum_{k=-\infty}^{\infty} x(t - kT_0) = \sum_{n=-\infty}^{\infty} x_n e^{jn\omega_0 t}$$

$$x(t) \leftrightarrow X(\omega)$$

$$x_n = \frac{1}{T_0} X(n\omega_0)$$

- 4) Apply the Fourier Transform theorems and properties to find  $X(\omega)$
- 5) Find signal power and energy using Parseval's theorem
- 6) Determine the Transfer Function of linear time invariant systems -  $H(\omega)$   
Finding  $H(\omega)$  from block diagram and/or LCCDE
- 7) Determine the output of an LTI system given its input
- 8) Understand the concept of bandwidth and the inverse signal duration/bandwidth relationship
  - First zero definition
  - 3 dB definition
  - Inverse time duration-bandwidth relationship
- 9) Criteria for an ideal linear time invariant system – Ideal Filters & Distortionless Transmission
  - a) Distortionless transmission  $y(t)=Kx(t-\tau)$   $H(\omega)=Ke^{-j\omega\tau}$  for all  $\omega$ .
  - b) Signal  $x(t)$  has bandwidth  $B_{\text{signal}}$  then distortionless transmission with respect to  $x(t)$  if  $H(\omega)$  has constant amplitude and linear phase ( $H(\omega)=Ke^{-j\omega\tau}$ ) over the signal bandwidth,  $B_{\text{signal}}$ .
  - c) ILPF  $\rightarrow H(\omega)=Ke^{-j\omega\tau}$  for system bandwidth,  $B_H$ .
  - d) IBPF, IBRF, IHPF
  - e) If  $B_{\text{System}} \gg B_{\text{signal}}$  then negligible distortion, where  $B_{\text{System}}$ =system bandwidth and  $B_{\text{signal}}$ =signal bandwidth
- 16) Basic modulation: DSB-SC, DSB-LC (AM), and FDM: Transmitters and Receivers
- 17) Sampling
  - a) Sampling Theorem
  - b) Sampling rate  $f_s > 2B$  (Nyquist sampling rate =  $2B$ )
  - c) Understanding the periodic nature of the spectrum of a sampled signal
  - d) Aliasing; causes and remedies
  - e) Recovery of  $x(t)$  from  $x_s(t)$  using an LPF

## 18) Discrete Time Signals and Systems

- a) Discrete signal notation, e.g.,  $x[n]=\{a, b, \underline{c}, d, \dots\}$  then  $x[0]=c$
- b) Discrete Time Signals  $u[n]$ ,  $\delta[n]$ ,  $\cos(\Omega n + \phi)$ ,  $p^n u[n]$   
where  $\Omega =$  the discrete-time angular frequency
- c) Discrete time LTI systems
  - Difference equations
  - ARMA format for difference equations
  - Block diagrams with delay blocks
  - Properties of Discrete Time Systems
    - o Linearity
      - Scaling
      - Additivity
    - o Time-invariance
    - o Memoryless (static) vs Memory (dynamic)
    - o BIBO stable
    - o Casual
    - o Discrete time impulse response,  $h[n]$

## 19) Discrete Time Convolution

## 20) z-transform

- a) Finding  $X(z)$  given  $x[n]$
- b) Finding  $x[n]$  given  $X(z)$
- c) Finding transfer function  $H(z)$  given
  - The impulse response
  - Difference equation
  - Block diagram
- d) Finding locations of poles and zeros of  $H(z)$
- e) Finding frequency response  $H(e^{j\Omega})$  and understanding its relationship to the unit circle.
- f) Finding the system output given input  $= A \cos(\Omega_{in} n + \phi)$